

# KEY RECOVERY OF PASSWORD-BASED AES-GCM WITH THE PARTITIONING ORACLE ATTACK

**Members:**  
Christian James Tan (NUS High School of Mathematics and Science)  
Xu Jingxin (Anglo-Chinese School (Independent))

**Mentors:**  
Ruth Ng Li Yung, Choo Jia Guang (DSO National Laboratories)

## 1) BACKGROUND ON AUTHENTICATED ENCRYPTION & COLLISIONS

### Authenticated Encryption (Symmetric scheme)

Encryption: ensures confidentiality (secrecy) - jumbles PT bytes to CT akin to random permutation  
MAC: ensures authenticity & integrity - that the message has not been illicitly changed

Encryption (encrypt-then-MAC)

- Encrypt PT to CT
- Generate a MAC of the CT and send it with CT

Decryption

- Authentication: recalculate MAC - compare it with received MAC
- Decryption fails if they don't match
- Then decrypt CT to get PT

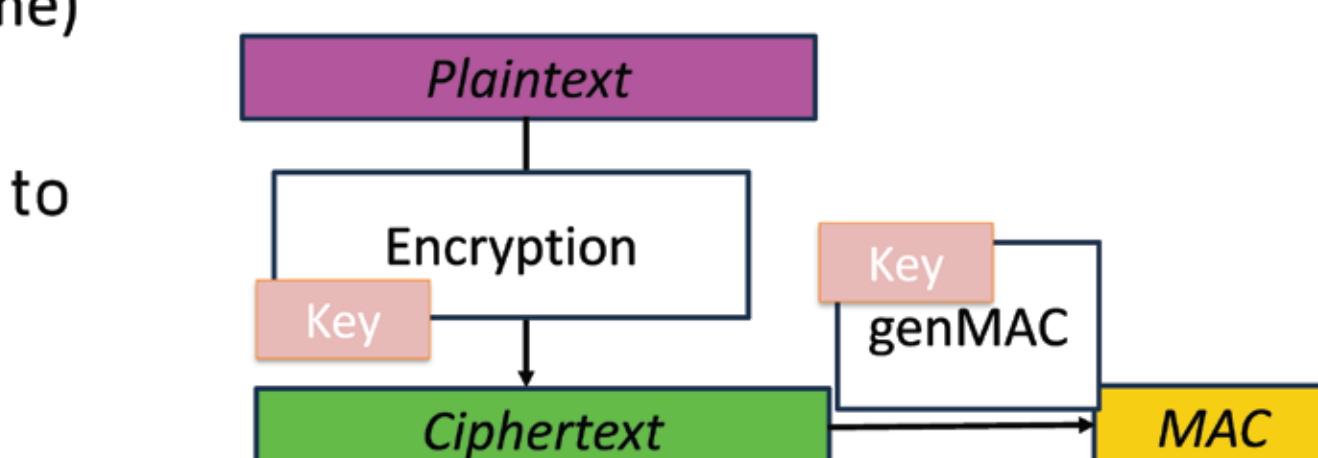


Fig 1.1: Encryption

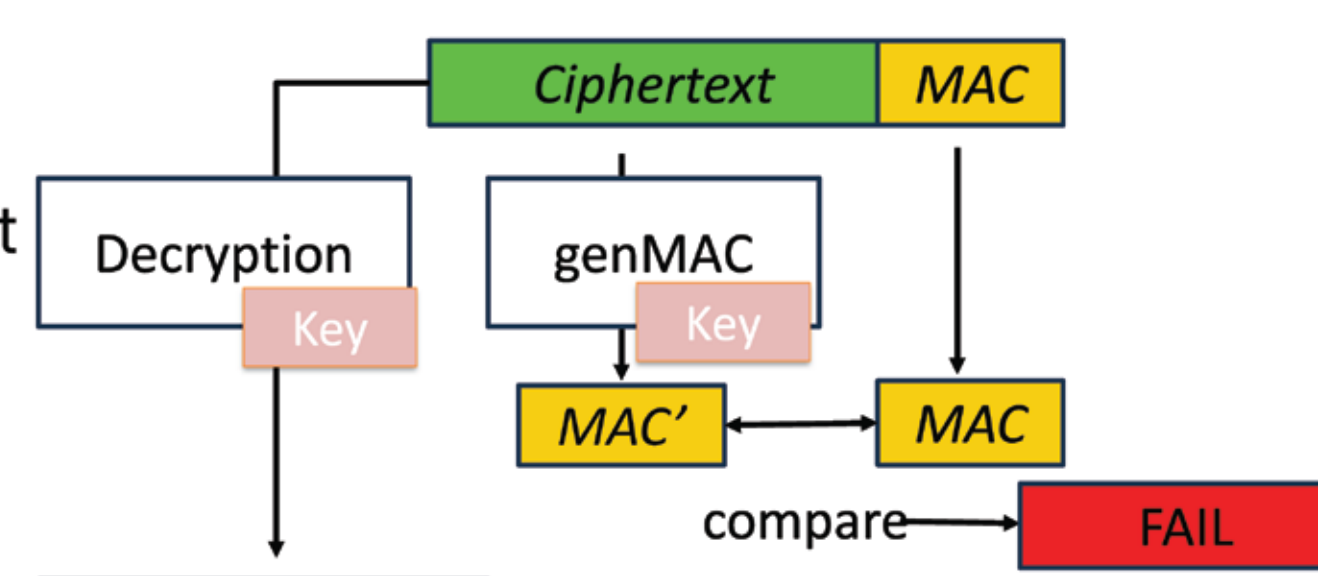


Fig 1.2: Decryption

### Key multi-collision

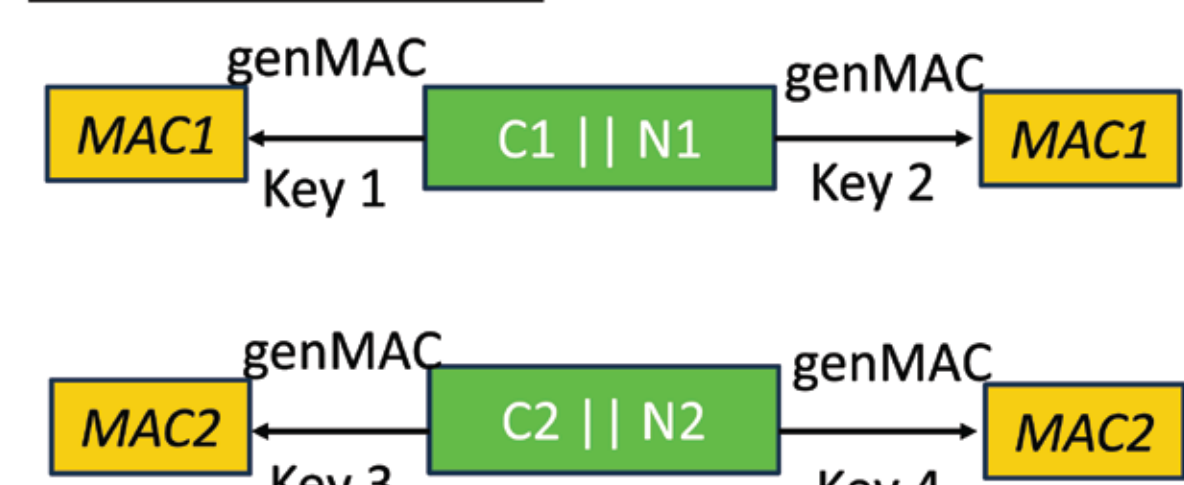


Fig 2: Collisions

- Same CT (and nonce) decrypts successfully under different keys.
- Colliding ciphertexts in non-key-committing schemes
- Multi-collisions: collide many keys

Examples of non-committing schemes

- GCM (Galois/Counter Mode)
- ChaCha20/Poly1305
- => MACs are polynomial based

## 3) IMPLEMENTATION DETAILS OF ATTACK

### Scenario description

- Messaging app
- Encrypt & sends messages using AES-GCM.
- Pre-shared passphrase used as the key in GCM
- Processing of ciphertext and MAC (and nonce): Authentication -> decryption -> decoding
- The receiver sends an acknowledgement message before exiting program (to confirm reception)
- => We can exploit this as our decryption oracle!

We used a password list of size 100 000 passwords with associated frequency data, and it takes an average of 11 guesses and a maximum of 17 to recover the key used, with collisions of up to 20,000 keys (<43ms).

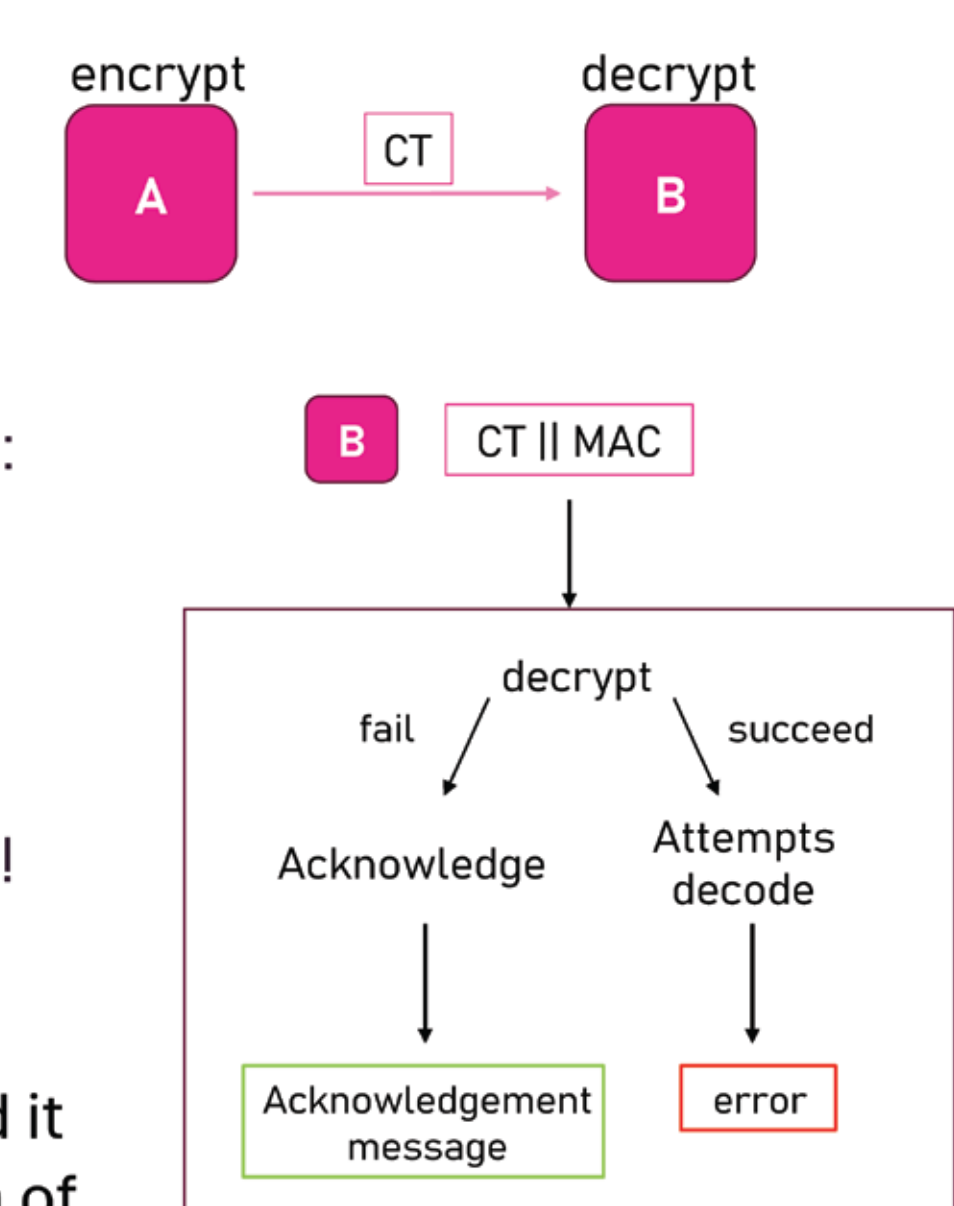


Fig 7: differentiating decryption failure/success

### Time complexity of attack

- For polynomial-based MACs e.g. GCM, construction of colliding ciphertexts is equivalent to polynomial interpolation:

$$\begin{aligned} \text{Naive } O(n^2) &\Rightarrow \sum_{i=1}^{\log(n)} \frac{O(n^2)}{2^i} \\ &= O(n^2) \end{aligned} \quad \begin{aligned} \text{Fast } O(n \log^2 n) &\Rightarrow \sum_{i=1}^{\log(n)} \frac{O(n \log^2 n)}{2^i} \\ &\approx O(n \log^2 n) \end{aligned}$$

- In fastest case, still  $O(n \log^2 n)$

## 2) PARTITIONING ORACLE ATTACK<sup>[1]</sup>

### Attack target: the Partitioning Oracle

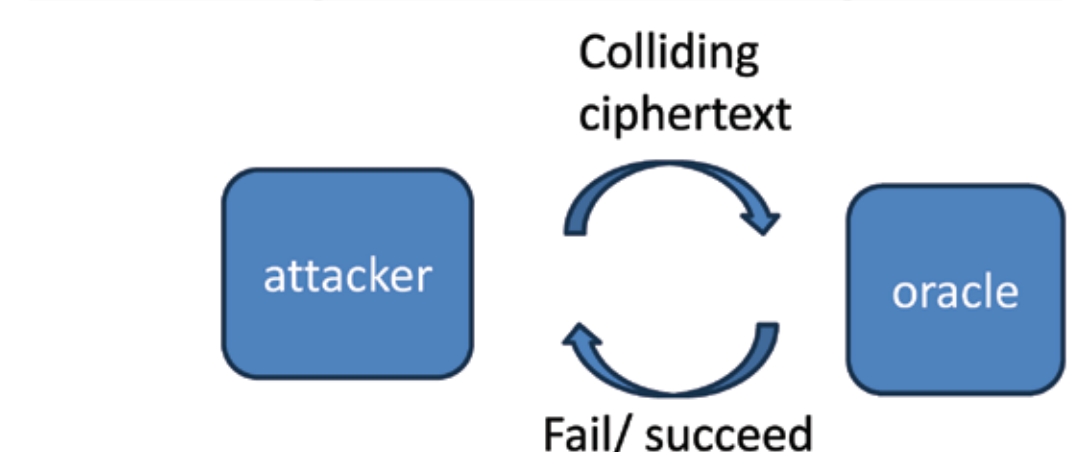


Fig 3: Partitioning Oracle

- Decryption oracle
- Indicates failure OR success of decryption.
- Some indicators eg error message, lack of response, timing side channels

### Attack procedure

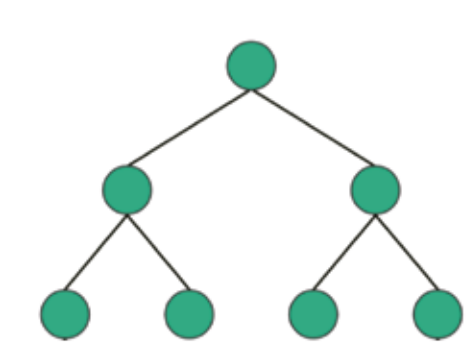


Fig 4: Binary tree

To leak the key used by a partitioning oracle:

- Compute a colliding ciphertext for a chosen set of 'colliding' keys.
- Query oracle and observe decryption status
  - If succeed: oracle's key is in set of 'colliding' keys
  - If fail: oracle's key is not in set (in complement of set).
- Compute next colliding ciphertext and repeat.
- => Attacker 'partitions' and narrows down the key space.
- Binary search (ideal) or linear scan in chunks followed by binary search (non-ideal)

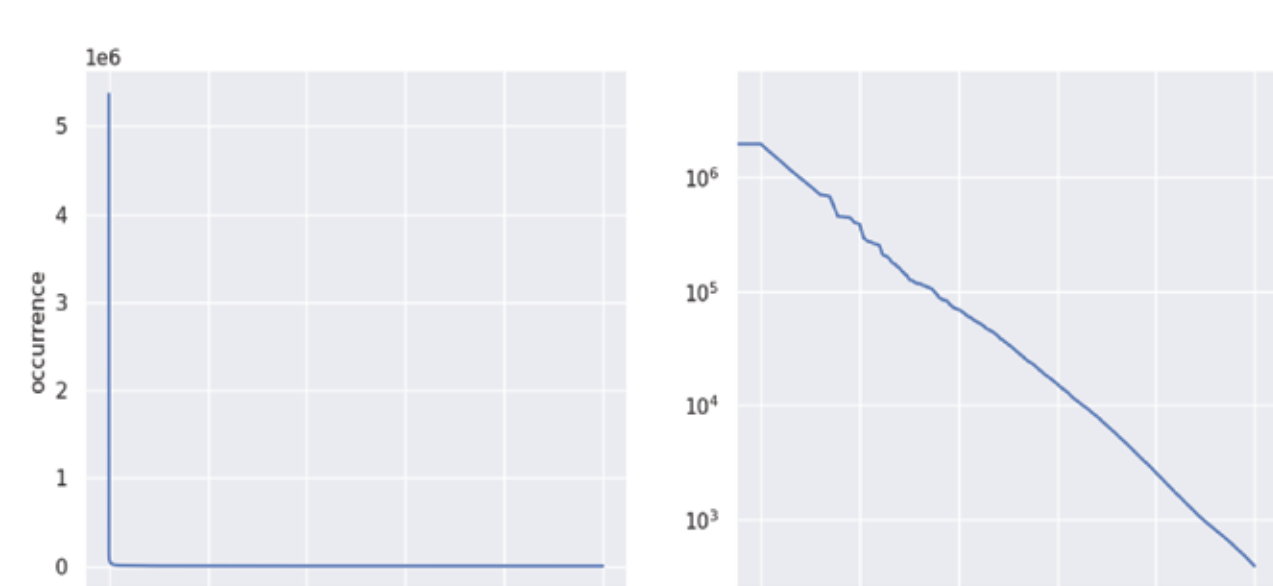


Fig 5: Zipfian distribution - rank and frequency in inverse proportion

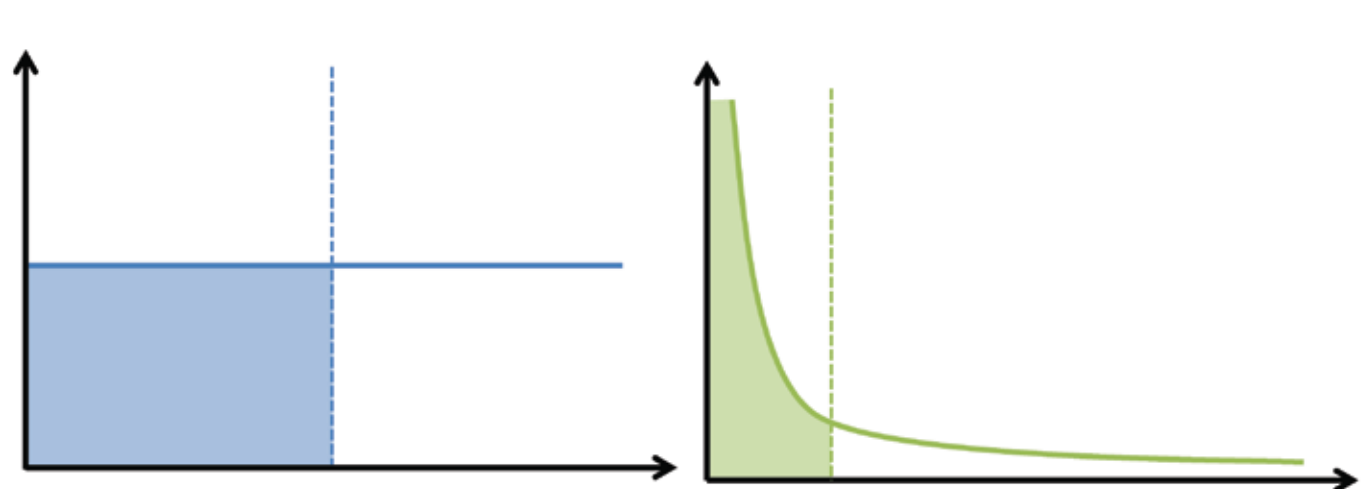


Fig 6: half the probability with fewer than half the keys.

### Password-derived keys

- Some keys are derived from passwords using keyderivation functions
- Passwords are non-uniformly distributed - instead, they follow a Zipfian distribution
- To partition the keyset in half (by probability), the colliding ciphertext requires fewer than half the keys
- Faster & more feasible construction of ciphertexts

## 4) CONDITIONS, APPLICATIONS & MITIGATIONS

Condition 1 scheme used is non-key-committing

- Use committing schemes. Eg HMAC
- Make schemes committing CTX<sup>[2]</sup>

Condition 2 Access to partitioning oracle:

- Hide information on decryption failure/success

Condition 3 (optional) Password-derived key

- Don't use a pre-shared passphrase
- Use uniformly generated random keys

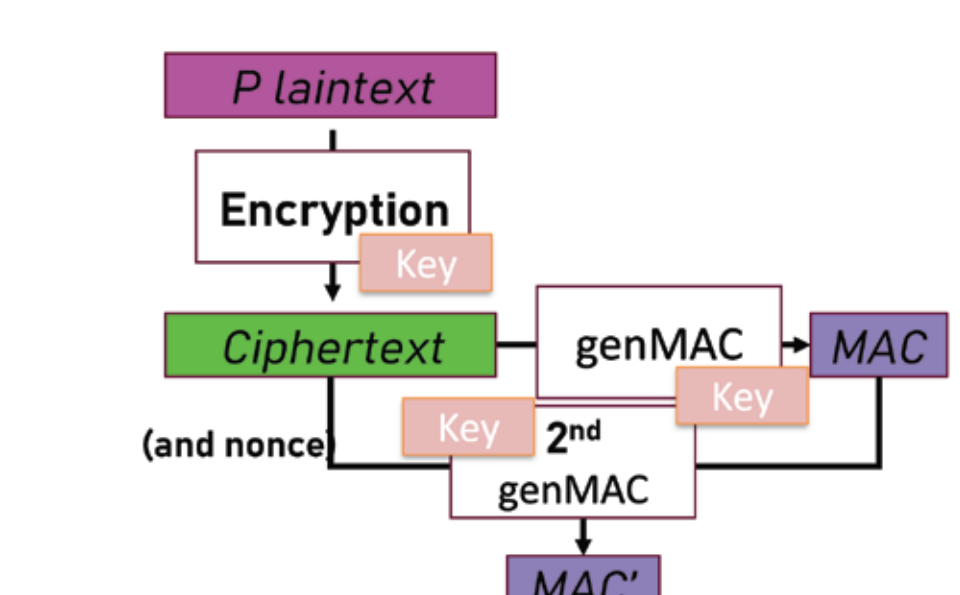


Fig 9: CTX transform

**Conclusion & further work:** This attack is a viable method of key-recovery due to the speedup it provides when the 3 conditions are met, as shown by our example, and can be applied to TLS (pre-shared key and GCM mode) in future work.

### Acknowledgements

We sincerely thank our mentors Ruth and Jia Guang, without whom this would have been impossible.

### References

- [1] Len, J., Grubbs, P., Ristenpart, T., 2021, Partitioning Oracle Attacks, 30th USENIX security symposium (USENIX Security 21): 195212.
- [2] Chan, J., Rogaway, P., 2022, On Committing Authenticated-Encryption, European Symposium on Research in Computer Security: 276294.